



Poker Cards Analysis - October 2022

The Directors

Entain Plc

This is to confirm that iTech Labs has examined the game logs for Poker games for the period **Oct 01, 2022 to Oct 31, 2022** as recorded by the respective game servers and analyzed the Poker cards for statistical randomness. The results of the analysis are given below.

For details on the gaming sites serviced by the Entain Plc game servers and used in this audit refer to the [List](#).

1. Poker hand types statistics

These calculations were done for Royal Flush, Straight Flush, Four of a Kind, Full House, Flush, Straight, 3 of a Kind, 2 pairs, 1 Pair, High Card.

The Poker hand types analysis involved creating subsets of data and conducting Chi-square tests on each subset.

The null hypothesis for the chi-square test is that the observed frequencies of each type of hand matches the theoretical values for a deck that has been shuffled using a perfect random number generator. The p-values observed in these multiple tests are expected to follow a uniform distribution for the range 0.0 to 1.0.

The analysis performs a KS Test (Kolmogorov-Smirnov test) for uniform distribution on the observed p-values, and the combined p-value result of this test is taken as the final result of the Poker hand types statistics tests.

1.1 Poker hand types statistics for 52 cards deck:

Test No.	DOF	ChiSqr	P-Value
1	9	22.28	0.00805
2	9	6.41	0.69800
3	9	7.02	0.63474
4	9	18.95	0.02563
5	9	7.25	0.61152
6	9	6.66	0.67254
7	9	6.52	0.68723
8	9	8.09	0.52504
9	9	6.18	0.72220
10	9	9.12	0.42604
11	9	13.28	0.15049
12	9	12.11	0.20732
13	9	12.21	0.20194
14	9	2.77	0.97262
15	9	6.89	0.64848
16	9	3.60	0.93575
17	9	3.22	0.95476
18	9	11.72	0.22932
19	9	11.75	0.22772
20	9	9.88	0.36031
21	9	11.70	0.23074
22	9	12.39	0.19244
23	9	19.29	0.02284
24	9	12.86	0.16917

25	9	2.53	0.98009
26	9	5.56	0.78325
27	9	5.81	0.75885
28	9	5.80	0.75972
29	9	5.40	0.79846
30	9	12.66	0.17883
31	9	22.46	0.00753
32	9	11.87	0.22076
33	9	12.74	0.17456
34	9	4.20	0.89752
35	9	6.48	0.69068
36	9	11.04	0.27266
37	9	6.06	0.73378
38	9	17.90	0.03630
39	9	24.56	0.00350
40	9	7.53	0.58189
41	9	10.96	0.27840
42	9	9.56	0.38765
43	9	5.57	0.78206
44	9	6.27	0.71238
45	9	4.35	0.88655
46	9	2.67	0.97603
47	9	17.66	0.03928
48	9	4.52	0.87383
49	9	7.40	0.59506
50	9	18.98	0.02539
51	9	5.86	0.75336
52	9	7.80	0.55424
53	9	9.41	0.40009
54	9	14.87	0.09465
55	9	5.88	0.75163
56	9	6.44	0.69489
57	9	7.67	0.56720
58	9	4.00	0.91139
59	9	7.48	0.58743
60	9	8.75	0.46103
61	9	15.70	0.07349
62	9	7.97	0.53713
63	9	6.95	0.64241
64	9	0.27	1.00000
65	9	11.31	0.25480
66	9	9.51	0.39175
67	9	10.58	0.30530
68	9	9.82	0.36517
69	9	5.08	0.82726
70	9	10.51	0.31073
71	9	9.03	0.43410
72	9	6.21	0.71880
73	9	5.24	0.81300
74	9	10.91	0.28199
75	9	10.38	0.32030
76	9	14.17	0.11646
77	9	9.17	0.42147
78	9	6.60	0.67840
79	9	14.16	0.11672

80	9	22.14	0.00845
81	9	14.01	0.12186
82	9	14.65	0.10088
83	9	4.41	0.88262
84	9	2.75	0.97354
85	9	10.15	0.33811
86	9	12.62	0.18048
87	9	9.85	0.36241
88	9	4.79	0.85237
89	9	17.41	0.04263
90	9	8.93	0.44330
91	9	5.36	0.80194
92	9	7.35	0.60026
93	9	9.79	0.36785
94	9	7.59	0.57549
95	9	8.71	0.46418
96	9	8.16	0.51768
97	9	5.81	0.75862
98	9	5.85	0.75450
99	9	8.21	0.51324
100	9	8.46	0.48894

Combined P-value for all tests (Using KS method)	0.97537
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Notes:

- 1) The P-values are observed probabilities from the Chi-Square tests. The last row shows the result of the KS Test performed on the p-values for all Chi-Square tests, where there are sufficient data.

1.2 Poker hand types statistics for 36 cards deck:

Test No.	DOF	ChiSqr	P-Value
1	8	7.17	0.51868
2	8	10.73	0.21744
Combined P-value for all tests (Using KS method)			N/A (Insufficient data)

Notes:

- 1) Since the number of samples available was insufficient to ensure at least 5 samples in the lowest probability hand type, (Royal Flush), the chi-square test has been performed by merging the Royal Flush and Straight Flush categories.
- 2) As the total number of tests (2) is insufficient to perform a meaningful KS Test, individual p-values from these tests are carried over to the next stage for combining using the Holm's method.

2. Poker rank statistics

The Poker rank analysis aims to establish that the rank of the cards in each position was equally distributed in one of the 13 possible ranks (2, 3, 4, 5, 6, 7, 8, 9, 10, J, Q, K, A) for a 52 card deck and 9 ranks (6, 7, 8, 9, 10, J, Q, K, A) for a 36 card deck.

The Poker rank analysis involved creating subsets of data and conducting Chi-square tests on each subset. The analysis performs a KS Test (Kolmogorov-Smirnov test) for uniform distribution on the observed p-values, and the combined p-value result of this test is taken as the final result of the Ranks statistics tests.

2.1 Poker rank statistics for 52 cards deck:

Test No.	Positions	DOF	ChiSqr	P-Value
1	7	84	84.12	0.47594
2	7	84	68.75	0.88569

3	7	84	96.09	0.17303
4	7	84	95.23	0.18897
5	7	84	86.92	0.39199
6	7	84	70.20	0.85934
7	7	84	86.18	0.41382
8	7	84	88.92	0.33589
9	7	84	77.15	0.68856
10	7	84	83.11	0.50683
11	7	84	92.63	0.24342
12	7	84	86.47	0.40502
13	7	84	82.04	0.54024
14	7	84	86.12	0.41554
15	7	84	87.65	0.37103
16	7	84	84.90	0.45215
17	7	84	85.42	0.43643
18	7	84	70.28	0.85764
19	7	84	79.51	0.61846
20	7	84	91.35	0.27343
21	7	84	85.29	0.44031
22	7	84	99.70	0.11629
23	7	84	83.06	0.50838
24	7	84	99.60	0.11761
25	7	84	96.11	0.17261
26	7	84	99.18	0.12338
27	7	84	77.98	0.66441
28	7	84	85.20	0.44295
29	7	84	96.05	0.17380
30	7	84	103.65	0.07180
31	7	84	82.96	0.51159
32	7	84	68.66	0.88720
33	7	84	94.23	0.20899
34	7	84	88.60	0.34452
35	7	84	81.93	0.54371
36	7	84	72.22	0.81673
37	7	84	95.39	0.18606
38	7	84	107.77	0.04135
39	7	84	78.67	0.64387
40	7	84	102.79	0.08013
41	7	84	70.20	0.85931
42	7	84	83.70	0.48863
43	7	84	80.45	0.58942
44	7	84	93.30	0.22845
45	7	84	85.31	0.43962
46	7	84	78.73	0.64196
47	7	84	83.86	0.48371
48	7	84	64.90	0.93945
49	7	84	64.43	0.94449
50	7	84	64.32	0.94561
51	7	84	109.98	0.03012
52	7	84	86.79	0.39567
53	7	84	81.40	0.56013
54	7	84	110.72	0.02704
55	7	84	55.54	0.99296
56	7	84	92.94	0.23657
57	7	84	87.16	0.38507

58	7	84	72.84	0.80239
59	7	84	106.83	0.04711
60	7	84	82.03	0.54036
61	7	84	80.73	0.58073
62	7	84	54.99	0.99399
63	7	84	98.83	0.12840
64	7	84	87.06	0.38787
65	7	84	74.62	0.75820
66	7	84	62.12	0.96481
67	7	84	104.59	0.06358
68	7	84	77.60	0.67535
69	7	84	100.81	0.10207
70	7	84	94.87	0.19597
71	7	84	83.65	0.49014
72	7	84	76.58	0.70485
73	7	84	87.96	0.36229
74	7	84	88.75	0.34042
75	7	84	81.64	0.55267
76	7	84	103.29	0.07522
77	7	84	69.66	0.86960
78	7	84	79.15	0.62927
79	7	84	75.10	0.74563
80	7	84	62.64	0.96084
81	7	84	100.16	0.11022
82	7	84	99.95	0.11301
83	7	84	89.85	0.31128
84	7	84	53.81	0.99578
85	7	84	79.55	0.61718
86	7	84	79.73	0.61164
87	7	84	65.76	0.92951
88	7	84	71.51	0.83251
89	7	84	67.61	0.90403
90	7	84	67.87	0.90004
91	7	84	85.20	0.44297
92	7	84	64.11	0.94777
93	7	84	83.70	0.48862
94	7	84	57.91	0.98668
95	7	84	92.30	0.25094
96	7	84	86.05	0.41739
97	7	84	91.26	0.27573
98	7	84	76.70	0.70137
99	7	84	72.65	0.80694
100	7	84	79.27	0.62553
Combined P-value for all tests (Using KS method)				0.97400

Notes:

- 1) The P-values are observed probabilities from the Chi-Square tests. The last row shows the result of the KS Test performed on the p-values for all Chi-Square tests, where there are sufficient data.

2.2 Poker rank statistics for 36 cards deck:

Test No.	Positions	DOF	ChiSqr	P-Value
1	7	56	67.45	0.14057
2	7	56	64.77	0.19741
3	7	56	46.35	0.81753
4	7	56	61.98	0.27151
5	7	56	48.10	0.76460
6	7	56	64.64	0.20042
7	7	56	66.53	0.15846
8	7	56	55.62	0.48912
9	7	56	62.64	0.25244
10	7	56	49.39	0.72137
11	7	56	60.71	0.31008
Combined P-value for all tests (Using KS method)				0.51723

Notes:

- 1) The P-values are observed probabilities from the Chi-Square tests. The last row shows the result of the KS Test performed on the p-values for all Chi-Square tests, where there are sufficient data.

3. Poker suits statistics

The Poker suits analysis aims to verify that that the cards dealt exhibit an equal probability of all 4 suits (Clubs, Diamonds, Hearts and Spades) in all positions.

The Poker suits analysis involved creating subsets of data and conducting Chi-square tests on each subset. The analysis performs a KS Test (Kolmogorov-Smirnov test) for uniform distribution on the observed p-values, and the combined p-value result of this test is taken as the final result of the Suits statistics tests.

3.1 Poker suits statistics for 52 cards deck:

Test No.	Positions	DOF	ChiSqr	P-Value
1	7	21	22.30	0.38232
2	7	21	23.70	0.30791
3	7	21	11.63	0.94912
4	7	21	18.84	0.59522
5	7	21	17.09	0.70576
6	7	21	27.10	0.16757
7	7	21	17.06	0.70754
8	7	21	18.43	0.62158
9	7	21	32.70	0.04968
10	7	21	31.90	0.05991
11	7	21	25.07	0.24415
12	7	21	24.38	0.27521
13	7	21	17.61	0.67330
14	7	21	12.39	0.92860
15	7	21	30.34	0.08536
16	7	21	28.08	0.13785
17	7	21	20.74	0.47474
18	7	21	17.19	0.69951
19	7	21	25.63	0.22073
20	7	21	24.63	0.26335
21	7	21	37.06	0.01657
22	7	21	9.61	0.98359

23	7	21	12.35	0.92968
24	7	21	12.62	0.92124
25	7	21	26.23	0.19794
26	7	21	14.20	0.86090
27	7	21	20.27	0.50446
28	7	21	15.71	0.78589
29	7	21	15.80	0.78093
30	7	21	11.14	0.95995
31	7	21	9.15	0.98795
32	7	21	27.92	0.14249
33	7	21	19.68	0.54141
34	7	21	23.40	0.32309
35	7	21	17.85	0.65866
36	7	21	18.95	0.58820
37	7	21	29.61	0.10017
38	7	21	22.81	0.35403
39	7	21	23.40	0.32291
40	7	21	19.71	0.53964
41	7	21	17.37	0.68839
42	7	21	18.39	0.62432
43	7	21	21.40	0.43478
44	7	21	22.57	0.36753
45	7	21	18.53	0.61541
46	7	21	16.63	0.73306
47	7	21	42.79	0.00334
48	7	21	15.20	0.81266
49	7	21	16.65	0.73231
50	7	21	15.20	0.81269
51	7	21	7.73	0.99619
52	7	21	15.80	0.78051
53	7	21	11.95	0.94106
54	7	21	25.46	0.22789
55	7	21	17.01	0.71068
56	7	21	24.01	0.29257
57	7	21	23.56	0.31491
58	7	21	22.24	0.38555
59	7	21	17.19	0.69941
60	7	21	29.19	0.10945
61	7	21	21.09	0.45360
62	7	21	19.03	0.58328
63	7	21	31.15	0.07113
64	7	21	24.59	0.26532
65	7	21	15.27	0.80908
66	7	21	24.08	0.28912
67	7	21	33.37	0.04227
68	7	21	40.99	0.00563
69	7	21	8.83	0.99052
70	7	21	19.48	0.55469
71	7	21	17.77	0.66371
72	7	21	30.17	0.08862
73	7	21	24.15	0.28599
74	7	21	13.49	0.89064
75	7	21	18.02	0.64788
76	7	21	18.83	0.59599
77	7	21	12.98	0.90918

78	7	21	21.19	0.44765
79	7	21	19.58	0.54778
80	7	21	14.20	0.86108
81	7	21	21.72	0.41605
82	7	21	13.58	0.88694
83	7	21	14.69	0.83832
84	7	21	18.74	0.60201
85	7	21	15.27	0.80920
86	7	21	26.92	0.17360
87	7	21	29.95	0.09291
88	7	21	18.20	0.63654
89	7	21	22.77	0.35638
90	7	21	24.36	0.27617
91	7	21	18.84	0.59566
92	7	21	24.37	0.27536
93	7	21	16.30	0.75277
94	7	21	17.37	0.68857
95	7	21	39.75	0.00796
96	7	21	10.89	0.96485
97	7	21	22.37	0.37820
98	7	21	29.31	0.10680
99	7	21	22.42	0.37544
100	7	21	15.55	0.79423
Combined P-value for all tests (Using KS method)				0.63996

Notes:

- 1) The P-values are observed probabilities from the Chi-Square tests. The last row shows the result of the KS Test performed on the p-values for all Chi-Square tests, where there are sufficient data.

3.2 Poker suits statistics for 36 cards deck:

Test No.	Positions	DOF	ChiSqr	P-Value
1	7	21	19.56	0.54926
2	7	21	18.16	0.63886
3	7	21	29.15	0.11040
4	7	21	21.77	0.41298
5	7	21	11.59	0.94998
6	7	21	15.30	0.80781
7	7	21	18.32	0.62867
8	7	21	15.58	0.79255
9	7	21	21.27	0.44244
10	7	21	24.56	0.26672
11	7	21	39.88	0.00770
Combined P-value for all tests (Using KS method)				0.97184

Notes:

- 1) The P-values are observed probabilities from the Chi-Square tests. The last row shows the result of the KS Test performed on the p-values for all Chi-Square tests, where there are sufficient data.

4. Summary of the analysis

4.1 Summary of the analysis of 52 cards deck:

The analysis of 52 cards completes by combining the result of the KS Test performed in the 3 types of analysis (Hand Types, Ranks and Suits) for 52 card decks using the Holm's method and producing a single Combined P -value.

The combined p-value produced using the Holm's method is used as indication for statistical randomness.

Combination of p-values using Holm's Method		
Test	P-Value	P-Adjusted
Ranks Test	0.97400	1.00000
Suits Test	0.63996	1.00000
HandTypes Test	0.97537	1.00000
Combined P-Value using Holm's Method		1.00000

Notes:

- 1) The combined p-value of all statistical tests using Holm's Method conducted for 52 card decks is greater than the minimum value of 0.05 which indicates that the randomness of the observed data falls within 95% confidence limits.

The final outcome of the analysis of 52 cards deck indicates that the RNG is working correctly.

4.2 Summary of the analysis of 36 cards deck:

The analysis of 36 cards completes by combining the result of the KS Test performed in the 3 types of analysis (Hand Types, Ranks and Suits) for 36 card decks using the Holm's method and producing a single Combined P -value. Where there are insufficient data the individual Chi-Square tests results are used in the Holm's method for producing a combined p-value.

The combined p-value produced from the using the Holm's method is used as indication for statistical randomness.

Combination of p-values using Holm's Method		
Test	P-Value	P-Adjusted
Ranks Test	0.51723	1.00000
Suits Test	0.97184	1.00000
HandTypes Test	0.51868	1.00000
HandTypes Test	0.21744	0.86977
Combined P-Value using Holm's Method		0.86977

Notes:

- 1) The combined p-value of all statistical tests using Holm's Method conducted for 36 card decks is greater than the minimum value of 0.05 which indicates that the randomness of the observed data falls within 95% confidence limits.

The final outcome of the analysis of 36 cards deck indicates that the RNG is working correctly.

5. Conclusion

Analysis of actual data from game logs for 'Hand Types', 'Ranks' and 'Suits' for **52-card decks** and **36-card decks** indicated statistical randomness.

iTech Labs has done limited sanity checks to verify the integrity of the game logs. iTech Labs also maintains a copy of the game logs for verification purposes. There were a large enough number of game records to give the calculations sufficient statistical power.

We conclude that the Random Number Generator (RNG) is working correctly.

Please click here to see the [Original](#) report.

Signed:



Kiren Sreekumar
Principal Consultant
iTech Labs Australia
Date: 14 Oct 2022

Signed:



Geoff Nicoll
Principal Consultant
iTech Labs Australia
Date: 14 Oct 2022

Disclaimer.

While it is not possible to test all possible scenarios in a laboratory environment, iTech Labs has conducted a level of testing appropriate for a component test of this type.

